

**WARM UP:**

I have a confidence interval for a mean that is (50.84, 53.76)

(a) What is the sample mean?

(b) What is the margin of error?

(c) Assuming the sample size is 40 and the sample standard deviation is 4.3, what is the level of confidence?

**WARM UP:**

I have a confidence interval for a mean that is (50.84, 53.76)

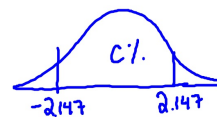
(a) What is the sample mean?  $\bar{x} = 52.3$

(b) What is the margin of error?  $m = 1.46$

(c) Assuming the sample size is 40 and the sample standard deviation is 4.3, what is the level of confidence?

$$1.46 = t^* \left( \frac{4.3}{\sqrt{40}} \right)$$

$$t^* = 2.147$$



$$P(-2.147 < t < 2.147) = 96.19\%$$

$$t.cdf(-2.147, 2.147, 39) =$$

**Ch. 24: Comparing 2 means**

2-sample t-test and interval

**2-Sample t-Test****HYPOTHESES:**

$$H_0: \mu_1 = \mu_2 \quad \text{OR} \quad \mu_1 - \mu_2 = 0$$

$$H_a: \mu_1 \geq \mu_2 \quad \text{OR} \quad \mu_1 - \mu_2 \geq 0$$

**CONDITIONS:**

- just double the 1-sample conditions

(1) 2 independent SRS ① comment on both SRS + indep

(2)  $\text{pop}_1 \geq 10 \cdot n_1$   
 $\text{pop}_2 \geq 10 \cdot n_2$

② comment on both pop

(3) 2 normal populations or  
 $n_1$  and  $n_2 \geq 30$

③ check/comment on both

Conditions met  $\Rightarrow$  Use t-distribution  $\rightarrow$  2-sample t-Test

**MECHANICS:**

Test statistic:

$$t = \frac{\text{statistic} - \text{parameter}}{\text{Std. dev. of statistic (SE)}} \quad t = \frac{(\bar{x}_1 - \bar{x}_2)}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$$

$$\text{P-value: } P(t \geq \text{test stat}) = t.cdf(\text{LB}, \text{UB}, \text{df})$$

on calculator: 2 Samp T-Test

df = on calculator! **OR** use the smaller df of the 2 samples

Round nearest  
#

$$\begin{array}{l} n_1 = 45 \\ df = 44 \end{array} \quad \begin{array}{l} n_2 = 53 \\ df = 52 \end{array}$$

**CONCLUSION:** (Same 2 sentences)

- reject/fail to reject  $H_0$ ....

- sufficient/insufficient evidence of  $H_a$

**Example:** Resting pulse rates for a random sample of 26 smokers had a mean of 80 beats per minute (bpm) and a standard deviation of 5 bpm. Among 32 randomly chosen nonsmokers, the mean and standard deviation were 74 and 6 bpm. Both sets of data were roughly symmetric and had no outliers. Is there evidence of a difference in mean pulse rate between smokers and non-smokers?

Hypotheses:

$$H_0: \mu_s = \mu_n$$

$$H_a: \mu_s \neq \mu_n$$

$$n_N = 32 \quad n_s = 26$$

$$\bar{x}_N = 74 \quad \bar{x}_s = 80$$

$$s_N = 6 \quad s_s = 5$$

CONDITIONS:

- ① 2 indep SRS
  - ②  $pop_s \geq 10 n_s$   
 $pop_n \geq 10 n_n$
  - ③ 2 normal pop's  
or  
 $n_1$  and  $n_2 \geq 30$
- ① Stated both random samples. Assume smokers indep. of non-smokers.
- ② Assumed more than 260 smokers & 320 non-smokers.
- ③  $n_N = 32 \geq 30$   
Stated both sets of data symm w/ no outliers → assumed normal distrib.

MECHANICS: Cond. met → t distrib → 2 sample t test

$$t = \frac{80 - 74}{\sqrt{\frac{5^2}{26} + \frac{6^2}{32}}} = 4.154$$

$$2P(t > 4.154 | df = 56) = 1.129 \times 10^{-4}$$

from calculator when we do 2 samp t test

CONCLUSION:

We reject  $H_0$  b/c p-value of  $1.129 \times 10^{-4} < \alpha = 0.05$ .

We have suff. evid. that the avg. resting pulse rate of smokers is not equal to non-smokers.

## 2-sample t-Interval:

CONDITIONS: same as 2-sample test

Conditions met → Use T-distribution → 2 sample t- Interval

MECHANICS:

statistic ± (critical value)(std. dev. of statistic)

$$(\bar{x}_1 - \bar{x}_2) \pm t^* \left( \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}} \right) = (a, b)$$

true diff. btw.  $\mu_1$  and  $\mu_2$

↑  
INVT

on calculator: 2 Samp T-Int

df = on calculator

CONCLUSION:

We are \_\_\_\_% confident that the difference between the averages of \_\_\_\_ and \_\_\_\_ is between \_\_\_\_ and \_\_\_\_ units.

\*\* Is 0 in the interval???

no diff. btw.  $\mu_1, \mu_2$   
(-, +)

Do the confidence interval for our smoking example earlier to estimate the difference. Use 95% confidence.

Conditions met --> t distribution --> 2 sample t Interval Mechanics:

$$(80-74) \pm (2.0032) \sqrt{\frac{5^2}{26} + \frac{6^2}{32}} = (3.1063, 8.8937)$$

df = 56  
n = 57  
↑ INVT

Conclusion:  
We are 95% confident that the difference between the avg resting pulse rate of smokers and non smokers is between 3.1063 bpm and 8.8937 bpm.

**Example 2:** Here are the saturated fat content (in grams) for several pizzas sold by two national chains. Do the two pizza chains have significantly different mean saturated fat contents? If so, complete an interval to estimate the difference.

Brand D	17	12	10	8	8	10	10	5	16	16
	8	12	15	7	11	11	13	13	11	12
Brand PJ	6	7	11	9	4	4	7	9		
	11	3	4	5	8	5	5			

2 Samp t Test  
Data  
L1  
L2

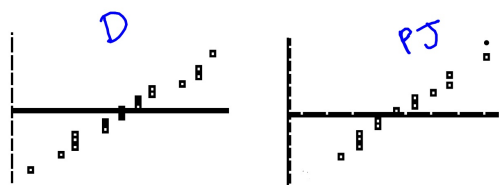
Hypotheses:

$$H_0 : \mu_D = \mu_{PJ}$$

$$H_A : \mu_D \neq \mu_{PJ}$$

**Conditions:**

- 2 independent SRS
  - assumed representative, & brand D and brand PJ are assumed to be indep.
- $pop_1 \geq 10n_1$   
 $pop_2 \geq 10n_2$ 
  - there are more than 200 brand D pizzas and 150 brand PJ pizzas sold.
- 2 normal populations or  $n_1$  and  $n_2 \geq 30$ 
  - normal probability plots of both samples are approx. linear  
--> both have norm distributions



Conditions met --> use t-distribution --> 2-samp t-test Mechanics:

$$n_D = 20 \quad \bar{x}_D = 11.25 \quad s_D = 3.193 \quad \alpha = 0.05$$

$$n_{PJ} = 15 \quad \bar{x}_{PJ} = 6.53 \quad s_{PJ} = 2.588$$

df = 33

$$t = \frac{11.25 - 6.533}{\sqrt{\frac{(3.193)^2}{20} + \frac{(2.588)^2}{15}}} = 4.823$$

$$2 * P(t > 4.823) = 3.151 \times 10^{-5} = 0.0000315$$

Conclusion:

We reject  $H_0$  b/c p-value of  $0.00003 < \alpha = 0.05$ .

We have sufficient evidence that the average saturated fat content of brand D is not equal to brand PJ.

Interval:

Conditions met --> t-distribution --> 2 sample t interval

df = 33

$$(11.25 - 6.533) \pm (2.0345) \sqrt{\frac{(3.193)^2}{20} + \frac{(2.588)^2}{15}} = (2.7266, 6.7067)$$

We are 95% confident that the difference between the average saturated fat content of brand PJ and brand D is between 2.7266 and 6.7067 grams.

HW:

p. 579 #2, 3, 11, 14, 27, 36 (a only)